Package: personnelSelectionUtility (via r-universe)

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Title Utility Analysis Methods for Personnel Selection

Version 1.0.2

Description Implements classical and contemporary utility-analysis methods for personnel selection, organised by criterion scale (classification or continuous/monetary) and selection structure (compensatory or multiple-hurdle). Methods include Taylor-Russell classification (Taylor and Russell, 1939, <doi:10.1037/h0057079>), Brogden-Cronbach-Gleser monetary utility (Brogden, 1949, <doi:10.1111/j.1744-6570.1949.tb01397.x>), Schmidt-Hunter-Pearlman intervention utility (Schmidt and others, 1979, <doi:10.1037/0021-9010.64.6.609>), Sturman comprehensive cascade (Sturman, 2001, <doi:10.1108/eb029072>), Thomas-Owen-Gunst multivariate classification (Thomas and others, 1977, <doi:10.3102/10769986002001055>), compensatory versus multiple-hurdle simulation (Ock and Oswald, 2018, <doi:10.1027/1866-5888/a000205>), AUC-to-effect-size conversions (Salgado, 2018, <doi:10.5093/ejpalc2018a5>), Pareto frontiers for validity-diversity trade-offs, and Monte Carlo uncertainty propagation.

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URL `https://github.com/rgempp/personnelSelectionUtility`, `https://gempp.cl/personnelSelectionUtility/`

BugReports `https://github.com/rgempp/personnelSelectionUtility/issues`

Depends R (>= 4.1.0)

Imports mvtnorm, stats

Suggests knitr, rmarkdown, testthat (>= 3.0.0)

VignetteBuilder knitr

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Contents

`adverse_impact_ratio` *Adverse-impact ratio by group*

Description

Computes selection rates and adverse-impact ratios by group. If no reference group is supplied, the highest selection-rate group is used as reference.

Usage

```
adverse_impact_ratio(selected, group, reference = NULL)
```

Arguments

`selected`	Logical or 0/1 vector indicating selection.
`group`	Group membership vector.
`reference`	Optional reference group.

Value

A data frame with selection rates and ratios.

References

De Corte, W., Lievens, F., & Sackett, P. R. (2007). Combining predictors to achieve optimal trade-offs between selection quality and adverse impact. Journal of Applied Psychology, 92, 1380-1393.

Pyburn, K. M., Ployhart, R. E., & Kravitz, D. A. (2008). The diversity- validity dilemma: Overview and legal context. Personnel Psychology, 61, 143-151.

Examples

```
# Literature: Pyburn, Ployhart, and Kravitz (2008); De Corte et al. (2007).
adverse_impact_ratio(c(1, 0, 1, 1, 0, 0), c("A", "A", "A", "B", "B", "B"))
```

---

argument_glossary *Argument naming glossary*

Description

Returns the package's recommended argument names and the notation they map to in the utility-analysis literature. The glossary is intended to make the API explicit and to avoid mixing compact statistical notation with readable R argument names.

Usage

```
argument_glossary()
```

Value

A data frame with argument names, literature notation, and usage notes.

References

Sturman, M. C. (2001). Utility analysis for multiple selection devices and multiple outcomes. Journal of Human Resource Costing and Accounting, 6(2), 9-28.

Holling, H. (1998). Utility analysis of personnel selection: An overview and empirical study based on objective performance measures. Methods of Psychological Research Online, 3(1), 5-24.

Examples

```
# Literature: Holling (1998); Sturman (2001).
argument_glossary()
subset(argument_glossary(), argument %in% c("base_rate", "selection_ratio", "sdy"))
```

`auc_to_d_equal_variance` *Convert AUC to Cohen's d under the equal-variance binormal model*

Description

Converts AUC to Cohen's d using $d = \sqrt{2}\Phi^{-1}(AUC)$. This conversion assumes two normal distributions with equal variances and should therefore be interpreted as a model-based effect-size conversion, not as a universal transformation from classifier accuracy to personnel-selection validity.

Usage

```
auc_to_d_equal_variance(auc)
```

Arguments

`auc`	Area under the ROC curve. Must be in `(0, 1)` because AUC values of 0 or 1 imply infinite d under the equal-variance binormal model.

Value

Numeric vector of Cohen's d values.

References

Hanley, J. A., & McNeil, B. J. (1982). The meaning and use of the area under a receiver operating characteristic (ROC) curve. *Radiology*, 143(1), 29-36.

Rice, M. E., & Harris, G. T. (2005). Comparing effect sizes in follow-up studies: ROC area, Cohen's d, and r. *Law and Human Behavior*, 29(5), 615-620.

Salgado, J. F. (2018). Transforming the area under the normal curve (AUC) into Cohen's d, Pearson's r_pb, odds-ratio, and natural log odds-ratio: Two conversion tables. *The European Journal of Psychology Applied to Legal Context*, 10(1), 35-47.

Examples

```
# Minimal example based on the equal-variance binormal conversion.
auc_to_d_equal_variance(.75)

# Direction is preserved: AUC below .50 implies a negative effect.
auc_to_d_equal_variance(.40)
```

`auc_to_point_biserial` *Convert AUC to a point-biserial correlation*

Description

Converts AUC to Cohen's d under the equal-variance binormal model and then converts d to a point-biserial correlation for a user-specified base rate. This is the preferred correlation-like conversion when a utility-analysis function requires a validity input but the available evidence is reported as AUC.

Usage

```
auc_to_point_biserial(auc, base_rate = 0.5)
```

Arguments

`auc`	Area under the ROC curve. Must be in `(0, 1)` because AUC values of 0 or 1 imply infinite d under the equal-variance binormal model.
`base_rate`	Proportion in the focal or successful group, usually denoted p. Must be in `(0, 1)`. The default is `.50`.

Value

Numeric vector of point-biserial correlations.

References

Hanley, J. A., & McNeil, B. J. (1982). The meaning and use of the area under a receiver operating characteristic (ROC) curve. *Radiology*, 143(1), 29-36.

Rice, M. E., & Harris, G. T. (2005). Comparing effect sizes in follow-up studies: ROC area, Cohen's d, and r. *Law and Human Behavior*, 29(5), 615-620.

Salgado, J. F. (2018). Transforming the area under the normal curve (AUC) into Cohen's d, Pearson's r_pb, odds-ratio, and natural log odds-ratio: Two conversion tables. *The European Journal of Psychology Applied to Legal Context*, 10(1), 35-47.

Examples

```
# Minimal example: AUC to d, then to r_pb for a balanced binary criterion.
auc_to_point_biserial(.75)

# Substantive example: examine how base rate affects the implied r_pb.
auc_to_point_biserial(.75, base_rate = c(.50, .30, .20, .10))
```

auc_to_rank_biserial *Convert AUC to a rank-biserial correlation*

Description

Converts the area under the ROC curve to the rank-biserial correlation, $r_{rb} = 2AUC - 1$. This is a distribution-free dominance summary: it rescales the probability that a randomly chosen successful applicant is ranked above a randomly chosen unsuccessful applicant from the `[0, 1]` AUC scale to the `[-1, 1]` correlation-like scale.

Usage

```
auc_to_rank_biserial(auc)
```

Arguments

`auc`	Area under the ROC curve. Must be in `[0, 1]`.

Value

Numeric vector of rank-biserial correlations.

References

Hanley, J. A., & McNeil, B. J. (1982). The meaning and use of the area under a receiver operating characteristic (ROC) curve. *Radiology*, 143(1), 29-36.

Kerby, D. S. (2014). The simple difference formula: An approach to teaching nonparametric correlation. *Comprehensive Psychology*, 3, 11.IT.3.1.

Rice, M. E., & Harris, G. T. (2005). Comparing effect sizes in follow-up studies: ROC area, Cohen's d, and r. *Law and Human Behavior*, 29(5), 615-620.

Examples

```
# Minimal example: AUC = .50 implies no dominance.
auc_to_rank_biserial(.50)

# AUC = .75 means 75% favorable pairwise ordering; r_rb = .50.
auc_to_rank_biserial(.75)
```

bcg_utility *Brogden-Cronbach-Gleser utility*

Description

Computes classical Brogden-Cronbach-Gleser utility. By default the baseline is random selection (`baseline_validity = 0`), but an operating baseline can be supplied using `baseline_validity` and, optionally, `baseline_selection_ratio`.

Usage

```
bcg_utility(
  validity,
  selection_ratio,
  sdy,
  n_selected,
  tenure,
  cost = 0,
  baseline_validity = 0,
  baseline_selection_ratio = NULL
)
```

Arguments

- `validity` Validity of the focal selection system, usually denoted `r_xy`.
- `selection_ratio` Selection ratio of the focal system.
- `sdy` Standard deviation of job performance in monetary units, `SD_y`.
- `n_selected` Number of selected applicants, `N_s`.
- `tenure` Expected tenure or number of periods, `T`.
- `cost` Total cost of the focal system net of baseline costs, if relevant.
- `baseline_validity` Validity of the baseline system. Defaults to `0`.
- `baseline_selection_ratio` Selection ratio of the baseline system. If `NULL`, it is assumed to equal `selection_ratio`.

Value

A psu_bcg object.

References

Cronbach, L. J., & Gleser, G. C. (1965). Psychological tests and personnel decisions (2nd ed.). University of Illinois Press.

Brogden, H. E. (1946). On the interpretation of the correlation coefficient as a measure of predictive efficiency. Journal of Educational Psychology, 37, 65-76.

Brogden, H. E. (1949). When testing pays off. Personnel Psychology, 2, 171-183.

Sturman, M. C. (2001). Utility analysis for multiple selection devices and multiple outcomes. Journal of Human Resource Costing and Accounting, 6(2), 9-28.

Examples

```
# Literature: Brogden (1946, 1949); Cronbach and Gleser (1965); Sturman (2001).
# Use the first call as a minimal example; the longer block illustrates
# how to interpret the function in the substantive setting discussed in the literature.
# Minimal example (Brogden (1946, 1949); Cronbach and Gleser (1965); Sturman (2001)).
bcg_utility(validity = .35, selection_ratio = .20, sdy = 50000,
            n_selected = 100, tenure = 3, cost = 75000)

# Substantive example (Brogden, 1946, 1949;
# Cronbach and Gleser, 1965; Sturman, 2001).
# Use an operating baseline rather than random selection.
naive <- bcg_utility(.35, .20, 50000, n_selected = 100, tenure = 3, cost = 75000)
incremental <- bcg_utility(.35, .20, 50000, n_selected = 100, tenure = 3,
                           cost = 75000, baseline_validity = .20)
c(naive = naive$net_utility, incremental = incremental$net_utility)
```

---

boudreau_utility *Boudreau-style discounted utility*

Description

Computes discounted multi-period utility with optional value, tax, and cost adjustments. The expected standardized criterion gain can be supplied directly as `delta_z_y`, or computed from validity and selection-ratio parameters.

Usage

```
boudreau_utility(
  delta_z_y = NULL,
  validity = NULL,
  selection_ratio = NULL,
  baseline_validity = 0,
  baseline_selection_ratio = NULL,
  sdy,
  n_by_period = NULL,
  variable_value = 0,
  contribution_margin = NULL,
  variable_value_convention = c("paper_plus", "cost_rate"),
  tax_rate = 0,
  discount_rate = 0,
  cost_by_period = NULL,
```

```
  discount_costs = TRUE,
  n_t = NULL,
  cost_t = NULL
)
```

Arguments

- `delta_z_y` Expected incremental standardized criterion gain. If `NULL`, it is computed from `validity`, `selection_ratio`, `baseline_validity`, and `baseline_selection_ratio`.
- `validity` Focal validity, used when `delta_z_y` is `NULL`.
- `selection_ratio` Focal selection ratio, used when `delta_z_y` is `NULL`.
- `baseline_validity` Baseline validity. Defaults to zero.
- `baseline_selection_ratio` Baseline selection ratio. Defaults to `selection_ratio`.
- `sdy` Standard deviation of job performance in monetary units.
- `n_by_period` Vector of selected/retained employees in each period. This is the preferred v0.4.0 name for the literature's `N_t`.
- `variable_value` Boudreau-style multiplier `V`. By default the multiplier is `(1 + variable_value)`, matching the printed Boudreau-style notation. Set `variable_value_convention = "cost_rate"` to use `(1 - variable_value)`, or pass `contribution_margin` directly when the margin is known.
- `contribution_margin` Optional contribution-margin multiplier. Overrides `variable_value` when supplied.
- `variable_value_convention` Either `"paper_plus"` for `(1 + V)` or `"cost_rate"` for `(1 - V)`.
- `tax_rate` Tax rate.
- `discount_rate` Discount rate.
- `cost_by_period` Cost in each period. Scalar or vector matching `n_by_period`.
- `discount_costs` Should costs be discounted by period? Defaults to `TRUE`.
- `n_t` Legacy alias for `n_by_period`. Use `n_by_period` in new code.
- `cost_t` Legacy alias for `cost_by_period`. Use `cost_by_period` in new code.

Value

A `psu_boudreau` object.

References

Boudreau, J. W. (1983). Economic considerations in estimating the utility of human resource productivity improvement programs. Personnel Psychology, 36, 551-576.

Boudreau, J. W. (1991). Utility analysis for decisions in human resource management. In M. D. Dunnette & L. M. Hough (Eds.), Handbook of industrial and organizational psychology (Vol. 2, pp. 621-745). Consulting Psychologists Press.

Sturman, M. C. (2001). Utility analysis for multiple selection devices and multiple outcomes. Journal of Human Resource Costing and Accounting, 6(2), 9-28.

Holling, H. (1998). Utility analysis of personnel selection: An overview and empirical study based on objective performance measures. Methods of Psychological Research Online, 3(1), 5-24.

Examples

```
# Literature: Boudreau (1983, 1991); Sturman (2001); Holling (1998).
# Use the first call as a minimal example; the longer block illustrates
# how to interpret the function in the substantive setting discussed in the literature.
# Minimal example (Boudreau (1983, 1991); Sturman (2001); Holling (1998)).
boudreau_utility(validity = .35, selection_ratio = .20, sdy = 50000,
                 n_by_period = c(100, 90, 80), discount_rate = .08,
                 cost_by_period = c(75000, 10000, 10000))

# Substantive example (Boudreau, 1983, 1991;
# Sturman, 2001; Holling, 1998).
# Use an explicit contribution margin and operating baseline.
boudreau_utility(
  validity = .35,
  baseline_validity = .20,
  selection_ratio = .20,
  sdy = 50000,
  n_by_period = c(100, 90, 80, 70),
  contribution_margin = .30,
  tax_rate = .25,
  discount_rate = .08,
  cost_by_period = c(75000, 10000, 10000, 10000)
)
```

---

break_even_validity *Break-even validity for BCG utility*

Description

Solves the validity needed to obtain zero net utility under the BCG model.

Usage

```
break_even_validity(
  selection_ratio,
  sdy,
  n_selected,
  tenure,
  cost = 0,
  baseline_validity = 0
)
```

Arguments

`selection_ratio`
: Selection ratio.

`sdy`
: SDy.

`n_selected`
: Number selected.

`tenure`
: Expected tenure.

`cost`
: Cost.

`baseline_validity`
: Baseline validity.

Value

Required focal validity.

References

Boudreau, J. W. (1991). Utility analysis for decisions in human resource management. In M. D. Dunnette & L. M. Hough (Eds.), Handbook of industrial and organizational psychology (Vol. 2, pp. 621-745). Consulting Psychologists Press.

Holling, H. (1998). Utility analysis of personnel selection: An overview and empirical study based on objective performance measures. Methods of Psychological Research Online, 3(1), 5-24.

Examples

```
# Literature: Boudreau (1991); Holling (1998).
# Use the first call as a minimal example; the longer block illustrates
# how to interpret the function in the substantive setting discussed in the literature.
# Minimal example (Boudreau (1991); Holling (1998)).
break_even_validity(.20, 50000, 100, 3, cost = 75000)

# Substantive example (Boudreau, 1991; Holling, 1998).
# Required incremental validity under different costs.
costs <- c(25000, 75000, 150000)
setNames(
  break_even_validity(.20, 50000, 100, 3, cost = costs, baseline_validity = .15),
  paste0('cost_', costs)
)
```

---

coefficient_of_determination *Coefficient of determination*

Description

Computes the squared validity coefficient.

Usage

```
coefficient_of_determination(validity)
```

Arguments

`validity`	Predictor-criterion validity coefficient.

Value

Numeric vector with `validity^2`.

References

Taylor, H. C., & Russell, J. T. (1939). The relationship of validity coefficients to the practical effectiveness of tests in selection. Journal of Applied Psychology, 23, 565-578.

Holling, H. (1998). Utility analysis of personnel selection: An overview and empirical study based on objective performance measures. Methods of Psychological Research Online, 3(1), 5-24.

Examples

```
# Literature: Taylor and Russell (1939); Holling (1998).
coefficient_of_determination(.30)
```

---

compare_selection_systems

Compare compensatory and conjunctive multiple-hurdle selection systems

---

Description

Computes analytic compensatory expected performance and simulated multiple-hurdle expected performance using the same predictor/criterion correlation structure.

Usage

```
compare_selection_systems(
  predictor_cor,
  validities,
  compensatory_weights = NULL,
  compensatory_selection_ratio,
  hurdle_selection_ratios,
  n_sim = 1e+05,
  seed = NULL,
  n_applicants = NA_real_,
  compensatory_cost_per_applicant = 0,
  hurdle_cost_per_stage = 0,
  sdy = NULL,
  applicant_n = NULL
)
```

Arguments

- `predictor_cor` Predictor intercorrelation matrix.
- `validities` Vector of predictor-criterion correlations.
- `compensatory_weights` Weights for the compensatory composite.
- `compensatory_selection_ratio` Overall compensatory selection ratio.
- `hurdle_selection_ratios` Marginal selection ratios for hurdle stages.
- `n_sim` Number of simulated applicants for the hurdle system.
- `seed` Optional random seed.
- `n_applicants` Optional number of real applicants.
- `compensatory_cost_per_applicant` Cost per applicant for the compensatory system.
- `hurdle_cost_per_stage` Cost per applicant assessed at each hurdle.
- `sdy` Optional monetary value of one criterion standard deviation.
- `applicant_n` Legacy alias for `n_applicants`.

Value

A list with compensatory, multiple-hurdle, and difference summaries.

References

Ock, J., & Oswald, F. L. (2018). The utility of personnel selection decisions: Comparing compensatory and multiple-hurdle selection models. Journal of Personnel Psychology, 17(4), 172-182.

Examples

```
# Literature: Ock and Oswald (2018).
# Minimal example (Ock and Oswald (2018)).
Rxx <- matrix(c(1, .30, .30, 1), 2, 2)
compare_selection_systems(Rxx, c(.40, .30), hurdle_selection_ratios = c(.50, .50),
                          compensatory_selection_ratio = .25, n_sim = 1000, seed = 1)

# Substantive example with monetary utility.
compare_selection_systems(
  predictor_cor = Rxx,
  validities = c(.40, .30),
  compensatory_selection_ratio = .25,
  hurdle_selection_ratios = c(.50, .50),
  n_sim = 5000,
  seed = 123,
  n_applicants = 400,
  compensatory_cost_per_applicant = 800,
  hurdle_cost_per_stage = c(100, 300),
  sdy = 50000
)
```

`compare_selection_systems_staged` *Compare compensatory and staged multiple-hurdle selection systems*

Description

Compares a compensatory top-down composite against a staged multiple-hurdle system in which stages can be composites.

Usage

```
compare_selection_systems_staged(
  predictor_cor,
  validities,
  compensatory_weights = NULL,
  compensatory_selection_ratio,
  stage_predictors,
  stage_selection_ratios,
  stage_weights = NULL,
  n_sim = 1e+05,
  seed = NULL,
  n_applicants = NA_real_,
  compensatory_cost_per_applicant = 0,
  hurdle_cost_per_stage = 0,
  sdy = NULL,
  applicant_n = NULL
)
```

Arguments

`predictor_cor` Predictor intercorrelation matrix.

`validities` Vector of predictor-criterion correlations.

`compensatory_weights` Weights for the compensatory composite.

`compensatory_selection_ratio` Overall compensatory selection ratio.

`stage_predictors` List of integer vectors defining staged predictors.

`stage_selection_ratios` Within-stage selection ratios.

`stage_weights` Optional list of weight vectors.

`n_sim` Number of simulated applicants for the staged system.

`seed` Optional random seed.

`n_applicants` Optional number of real applicants.

`compensatory_cost_per_applicant`
: Cost per applicant for the compensatory system.

`hurdle_cost_per_stage`
: Cost per applicant assessed at each hurdle.

`sdy`
: Optional monetary value of one criterion standard deviation.

`applicant_n`
: Legacy alias for `n_applicants`.

Value

A list with compensatory, staged multiple-hurdle, and difference summaries.

References

Ock, J., & Oswald, F. L. (2018). The utility of personnel selection decisions: Comparing compensatory and multiple-hurdle selection models. Journal of Personnel Psychology, 17(4), 172-182.

Examples

```
# Literature: Ock and Oswald (2018).
# Use the first call as a minimal example; the longer block illustrates
# how to interpret the function in the substantive setting discussed in the literature.
# Minimal example (Ock and Oswald (2018)).
Rxx <- diag(4); Rxx[lower.tri(Rxx)] <- Rxx[upper.tri(Rxx)] <- .20
compare_selection_systems_staged(Rxx, validities = c(.40, .35, .20, .30),
  compensatory_selection_ratio = .20, stage_predictors = list(1:3, 4),
  stage_selection_ratios = c(.25, .80), n_sim = 1000, seed = 1)

# Substantive Ock-Oswald-style staged comparison.
compare_selection_systems_staged(
  predictor_cor = Rxx,
  validities = c(.40, .35, .20, .30),
  compensatory_weights = rep(1, 4),
  compensatory_selection_ratio = .20,
  stage_predictors = list(c(1, 3, 4), 2),
  stage_selection_ratios = c(.25, .80),
  n_sim = 5000,
  seed = 123,
  n_applicants = 500,
  compensatory_cost_per_applicant = 1000,
  hurdle_cost_per_stage = c(100, 900),
  sdy = 60000
)
```

`compensatory_selection` *Expected performance under compensatory top-down selection*

Description

Computes the expected standardized criterion performance of applicants selected on a weighted predictor composite. This is the compensatory cell of the package taxonomy: scores on stronger predictors can offset lower scores on weaker ones.

Usage

```
compensatory_selection(
  predictor_cor,
  validities,
  weights = NULL,
  selection_ratio,
  n_applicants = NA_real_,
  cost_per_applicant = 0,
  sdy = NULL,
  applicant_n = NULL
)
```

Arguments

- `predictor_cor` Predictor intercorrelation matrix, denoted `R_XX`.
- `validities` Vector of predictor-criterion correlations, denoted `r_xi,y`.
- `weights` Composite weights. Defaults to validity weights.
- `selection_ratio` Overall selection ratio for top-down selection on the composite.
- `n_applicants` Number of applicants, used for cost calculations. Preferred name in v0.4.0.
- `cost_per_applicant` Cost per assessed applicant.
- `sdy` Optional monetary value of one criterion standard deviation.
- `applicant_n` Legacy alias for `n_applicants`.

Value

A `psu_comparison` object.

References

Naylor, J. C., & Shine, L. C. (1965). A table for determining the increase in mean criterion score obtained by using a selection device. Journal of Industrial Psychology, 3, 33-42.

Ock, J., & Oswald, F. L. (2018). The utility of personnel selection decisions: Comparing compensatory and multiple-hurdle selection models. Journal of Personnel Psychology, 17(4), 172-182.

Examples

```
# Literature: Naylor and Shine (1965); Ock and Oswald (2018).
# Use the first call as a minimal example; the longer block illustrates
# how to interpret the function in the substantive setting discussed in the literature.
# Minimal example (Naylor and Shine (1965); Ock and Oswald (2018)).
Rxx <- matrix(c(1, .30, .30, 1), 2, 2)
compensatory_selection(Rxx, validities = c(.40, .30), selection_ratio = .20)

# Substantive example with costs and SDy.
Rxx <- matrix(c(
  1.00, .30, .20,
  .30, 1.00, .25,
  .20, .25, 1.00
), 3, 3, byrow = TRUE)
compensatory_selection(
  predictor_cor = Rxx,
  validities = c(.45, .35, .25),
  weights = c(1, 1, 1),
  selection_ratio = .20,
  n_applicants = 500,
  cost_per_applicant = 250,
  sdy = 60000
)
```

`composite_d` *Composite effect size for a weighted predictor battery*

Description

Computes Sackett-Ellingson-style composite d for a weighted battery.

Usage

```
composite_d(d, weights = NULL, predictor_cor = NULL, sd = NULL)
```

Arguments

`d`	Vector of standardized group differences or effect sizes.
`weights`	Composite weights. Defaults to equal weights.
`predictor_cor`	Predictor correlation matrix. Defaults to identity.
`sd`	Predictor standard deviations. Defaults to ones.

Value

Composite effect size.

References

Sackett, P. R., & Ellingson, J. E. (1997). The effects of forming multi- predictor composites on group differences and adverse impact. Personnel Psychology, 50, 707-721.

Examples

```
# Literature: Sackett and Ellingson (1997).
composite_d(d = c(.80, .30), weights = c(.7, .3),
            predictor_cor = matrix(c(1, .30, .30, 1), 2, 2))
```

---

cor_to_d *Convert a correlation to Cohen's d*

Description

Uses the common two-group approximation `d = 2r / sqrt(1 - r^2)`.

Usage

```
cor_to_d(r)
```

Arguments

r	Correlation coefficient.

Value

Cohen's d.

References

Schmidt, F. L., Hunter, J. E., & Pearlman, K. (1982). Assessing the economic impact of personnel programs on workforce productivity. Personnel Psychology, 35, 333-347.

Cohen, J. (1988). Statistical power analysis for the behavioral sciences (2nd ed.). Erlbaum.

Examples

```
# Literature: Cohen (1988); Schmidt, Hunter, and Pearlman (1982).
cor_to_d(.30)
```

`correct_r_direct_range_restriction`
Direct range-restriction correction for selection on the predictor

Description

Corrects a restricted validity coefficient for direct range restriction on the predictor using the standard Thorndike Case II expression.

Usage

```
correct_r_direct_range_restriction(
  r_restricted,
  range_restriction_ratio = NULL,
  u = NULL
)
```

Arguments

`r_restricted` Restricted-sample validity coefficient.

`range_restriction_ratio`
Ratio of unrestricted to restricted predictor standard deviations. This is the preferred v0.4.0 name for the literature's `u`.

`u` Legacy alias for `range_restriction_ratio`.

Value

Corrected validity coefficient.

References

Sackett, P. R., Laczo, R. M., & Arvey, R. D. (2002). The effects of range restriction on estimates of criterion interrater reliability: Implications for validation research. Personnel Psychology, 55, 807-825.

Ree, M. J., Carretta, T. R., Earles, J. A., & Albert, W. (1994). Sign changes when correcting for range restriction: A note on Pearson's and Lawley's selection formulas. Journal of Applied Psychology, 79, 298-301.

Lawley, D. N. (1943). A note on Karl Pearson's selection formulae. Proceedings of the Royal Society of Edinburgh, Section A, 62, 28-30.

Examples

```
# Literature: Lawley (1943); Sackett, Laczo, and Arvey (2002); Ree et al. (1994).
correct_r_direct_range_restriction(.25, range_restriction_ratio = 1.40)
correct_r_direct_range_restriction(.25, u = 1.40)
```

`correct_r_lawley` *Multivariate range-restriction correction (Lawley, 1943)*

Description

Corrects an observed (restricted) correlation matrix for direct selection on a subset of variables and incidental selection on the remaining variables, using Lawley's (1943) multivariate formulae.

Usage

```
correct_r_lawley(
  sigma_restricted,
  selection_indices,
  sigma_ss_unrestricted,
  standardize = TRUE
)
```

Arguments

`sigma_restricted`
: Observed (restricted) covariance or correlation matrix in the selected sample. Must be symmetric and positive semi-definite.

`selection_indices`
: Integer vector indicating which rows/columns of `sigma_restricted` correspond to variables on which selection was applied.

`sigma_ss_unrestricted`
: Unrestricted covariance submatrix for the selection variables (the same dimension as `sigma_restricted[selection_indices, selection_indices]`). Typically estimated from applicant-pool data.

`standardize`
: Logical. If `TRUE` (default), the corrected covariance matrix is converted to a correlation matrix via `stats::cov2cor()`.

Details

Let `S` index the variables on which selection was applied and `U` index the remaining (incidentally restricted) variables. Given the observed restricted covariance matrix `Sigma_star` and the unrestricted covariance submatrix `Sigma_SS_unrestricted` for the selection variables, Lawley's correction recovers the unrestricted covariance matrix:

$$\Sigma_{UV} = \Sigma^*_{UV} + \Sigma^*_{US} \left(\Sigma^*_{SS}\right)^{-1} \left(\Sigma_{SS} - \Sigma^*_{SS}\right) \left(\Sigma^*_{SS}\right)^{-1} \Sigma^*_{SV}$$
$$\Sigma_{UU} = \Sigma^*_{UU} + \Sigma^*_{US} \left(\Sigma^*_{SS}\right)^{-1} \left(\Sigma_{SS} - \Sigma^*_{SS}\right) \left(\Sigma^*_{SS}\right)^{-1} \Sigma^*_{SU}$$

for any partitioning into selection variables `S` and other variables `U,V`.

Sign changes flagged in `sign_changes` are not necessarily errors but should be inspected: Ree et al. (1994) documented that legitimate Lawley corrections can flip the sign of small predictor-criterion correlations when the restriction matrix is large.

Value

A list with components:

sigma_corrected The corrected (unrestricted) covariance or correlation matrix of the same dimension as `sigma_restricted`.

sigma_restricted The input restricted matrix (echoed).

selection_indices Indices treated as direct-selection variables.

incidental_indices Indices treated as incidentally restricted.

u Vector of `sd_restricted / sd_unrestricted` per selection variable, one of the standard summaries of restriction severity.

sign_changes Integer count of off-diagonal entries whose sign differs between corrected and observed matrices, flagged in the spirit of Ree, Carretta, Earles & Albert (1994).

References

Lawley, D. N. (1943). A note on Karl Pearson's selection formulae. *Proceedings of the Royal Society of Edinburgh, Section A*, 62, 28-30.

Mendoza, J. L., & Mumford, M. D. (1987). Corrections for attenuation and range restriction on the predictor. *Journal of Educational and Behavioral Statistics*, 12, 282-293.

Ree, M. J., Carretta, T. R., Earles, J. A., & Albert, W. (1994). Sign changes when correcting for range restriction: A note on Pearson's and Lawley's selection formulas. *Journal of Applied Psychology*, 79, 298-301.

Sackett, P. R., Lievens, F., Berry, C. M., & Landers, R. N. (2007). A cautionary note on the effects of range restriction on predictor intercorrelations. *Journal of Applied Psychology*, 92, 538-544.

Examples

```
# Three-variable example: selection on X1 (cognitive ability),
# incidental restriction on X2 (interview) and Y (criterion).
sigma_star <- matrix(c(
  1.00, 0.30, 0.25,
  0.30, 1.00, 0.20,
  0.25, 0.20, 1.00
), 3, 3)
# Unrestricted SD of X1 is larger; var increases by factor 1/u^2 = 1/.6^2
sigma_ss <- matrix(1 / 0.6^2, 1, 1)
correct_r_lawley(sigma_star, selection_indices = 1,
                 sigma_ss_unrestricted = sigma_ss)
```

`d_to_cor` *Convert Cohen's d to a correlation*

Description

Uses $r = d/\sqrt{d^2 + 4}$.

Usage

```
d_to_cor(d)
```

Arguments

d	Cohen's d.

Value

Correlation coefficient.

References

Schmidt, F. L., Hunter, J. E., & Pearlman, K. (1982). Assessing the economic impact of personnel programs on workforce productivity. Personnel Psychology, 35, 333-347.

Cohen, J. (1988). Statistical power analysis for the behavioral sciences (2nd ed.). Erlbaum.

Examples

```
# Literature: Cohen (1988); Schmidt, Hunter, and Pearlman (1982).
d_to_cor(.50)
```

---

d_to_point_biserial *Convert Cohen's d to a point-biserial correlation*

Description

Converts a standardized mean difference to the point-biserial correlation implied by a dichotomous criterion with base rate p. The implemented formula is $r_{pb} = d\sqrt{p(1-p)}/\sqrt{1+d^2p(1-p)}$. When `base_rate = .50`, this reduces to the common equal-group conversion $r = d/\sqrt{d^2+4}$.

Usage

```
d_to_point_biserial(d, base_rate = 0.5)
```

Arguments

d	Cohen's d. Must be numeric and finite.
base_rate	Proportion in the focal or successful group, usually denoted p. Must be in `(0, 1)`. The default is `.50`.

Value

Numeric vector of point-biserial correlations.

References

Cohen, J. (1988). *Statistical power analysis for the behavioral sciences* (2nd ed.). Erlbaum.

Rice, M. E., & Harris, G. T. (2005). Comparing effect sizes in follow-up studies: ROC area, Cohen's d, and r. *Law and Human Behavior*, 29(5), 615-620.

Salgado, J. F. (2018). Transforming the area under the normal curve (AUC) into Cohen's d, Pearson's r_pb, odds-ratio, and natural log odds-ratio: Two conversion tables. *The European Journal of Psychology Applied to Legal Context*, 10(1), 35-47.

Examples

```
# Minimal example: equal base-rate conversion equals d_to_cor().
d_to_point_biserial(.50, base_rate = .50)
d_to_cor(.50)

# Unequal base rates reduce the attainable point-biserial correlation.
d_to_point_biserial(.50, base_rate = c(.50, .20, .10))
```

---

disattenuate_correlation

Disattenuated correlation (Spearman, 1904)

Description

Corrects an observed correlation for unreliability in either or both variables.

Usage

```
disattenuate_correlation(r_observed, reliability_x = 1, reliability_y = 1)
```

Arguments

`r_observed`	Observed correlation.
`reliability_x`	Reliability of `X` (default 1, i.e., no correction).
`reliability_y`	Reliability of `Y` (default 1).

Value

Disattenuated correlation. Capped at +/- 1 with a warning when the algebraic value exceeds 1 in magnitude (typically a sign of unreliable reliability inputs).

References

Spearman, C. (1904). The proof and measurement of association between two things. *American Journal of Psychology*, 15, 72-101.

Examples

```
disattenuate_correlation(0.30, reliability_x = 0.80, reliability_y = 0.70)
```

`dominance_analysis` *Dominance analysis for predictor importance*

Description

Implements Budescu's (1993) dominance analysis to decompose the coefficient of determination of a multiple regression into contributions attributable to each predictor. Three dominance summaries are returned:

Usage

```
dominance_analysis(predictor_cor, predictor_criterion_cor)
```

Arguments

`predictor_cor` Predictor correlation matrix `R_xx`.

`predictor_criterion_cor`
Vector of predictor-criterion correlations `r_xy` (length `p`).

Details

- **Complete dominance**: predictor `i` *completely dominates* `j` if `R^2(S \cup {i}) > R^2(S \cup {j})` for every subset `S` not containing `i` or `j`. Reported as a pairwise dominance matrix.
- **Conditional dominance**: average increment of predictor `i` to `R^2` across subsets of size `k`, for `k = 0, ..., p-1`.
- **General dominance**: the average of conditional dominance values; equivalent to the Shapley value of `R^2`.

Value

A list with components:

r_squared_full The full-model `R^2`.

general_dominance Vector of length `p` whose entries sum to `r_squared_full`.

conditional_dominance `p x p` matrix; row `i` gives the average contribution of predictor `i` at subset sizes `0, 1, ..., p-1`.

complete_dominance `p x p` logical matrix where entry `[i,j]` is `TRUE` if `i` completely dominates `j`, `FALSE` if `j` completely dominates `i`, `NA` otherwise.

References

Azen, R., & Budescu, D. V. (2003). The dominance analysis approach for comparing predictors in multiple regression. *Psychological Methods*, 8, 129-148.

Budescu, D. V. (1993). Dominance analysis: A new approach to the problem of relative importance of predictors in multiple regression. *Psychological Bulletin*, 114, 542-551.

Examples

```
Rxx <- matrix(c(1, .30, .20,
                .30, 1, .25,
                .20, .25, 1), 3, 3)
rxy <- c(.40, .30, .25)
dominance_analysis(Rxx, rxy)
```

---

employee_flow   *Compute employee flows across periods*

Description

Computes retained headcount after hires and losses: `N_t = initial + cumsum(hired - lost)`.

Usage

```
employee_flow(hired, lost, initial = 0)
```

Arguments

`hired`	Number hired in each period.
`lost`	Number lost in each period.
`initial`	Initial headcount.

Value

Numeric vector of headcount by period.

References

Boudreau, J. W., & Berger, C. J. (1985). Decision-theoretic utility analysis applied to employee separations and acquisitions. Journal of Applied Psychology, 70, 581-612.

Boudreau, J. W. (1991). Utility analysis for decisions in human resource management. In M. D. Dunnette & L. M. Hough (Eds.), Handbook of industrial and organizational psychology (Vol. 2, pp. 621-745). Consulting Psychologists Press.

Examples

```
# Literature: Boudreau and Berger (1985); Boudreau (1991).
employee_flow(hired = c(100, 20, 20), lost = c(0, 30, 25))
```

forecasting_efficiency *Forecasting efficiency*

Description

Computes the proportional reduction in the standard error of prediction: `1 - sqrt(1 - validity^2)`.

Usage

```
forecasting_efficiency(validity)
```

Arguments

`validity`	Predictor-criterion validity coefficient.

Value

Numeric vector with forecasting efficiency values.

References

Holling, H. (1998). Utility analysis of personnel selection: An overview and empirical study based on objective performance measures. Methods of Psychological Research Online, 3(1), 5-24.

Examples

```
# Literature: Holling (1998).
forecasting_efficiency(.30)
```

fuse_composite_cor *Correlation matrix between several weighted composites*

Description

Given a stack of items and a weight matrix `W` whose columns are composite-specific weight vectors, computes the correlation matrix between the resulting composites under the standard Lord-Novick formula.

Usage

```
fuse_composite_cor(weights_matrix, item_cor)
```

Arguments

`weights_matrix`	`p x m` matrix; column `j` is the weight vector of composite `j`.
`item_cor`	`p x p` correlation matrix among items.

Value

m x m correlation matrix among composites.

Examples

```
R <- diag(4); R[lower.tri(R)] <- R[upper.tri(R)] <- .25
W <- cbind(c(1, 1, 0, 0), c(0, 0, 1, 1))
fuse_composite_cor(W, R)
```

---

fuse_reliability *Reliability of a weighted composite (Mosier, 1943; Lord & Novick, 1968)*

Description

Reliability of a weighted composite (Mosier, 1943; Lord & Novick, 1968)

Usage

```
fuse_reliability(weights, item_cor, item_reliabilities = NULL)
```

Arguments

weights	Numeric vector of composite weights.
item_cor	Symmetric correlation (or covariance) matrix among items.
item_reliabilities	Numeric vector of item reliabilities (length equal to weights). If NULL, the composite reliability is computed under the assumption that diagonal entries of item_cor are item reliabilities (e.g., when an empirical reliability matrix is supplied).

Value

The reliability of the weighted composite.

References

Lord, F. M., & Novick, M. R. (1968). *Statistical theories of mental test scores*. Addison-Wesley.

Mosier, C. I. (1943). On the reliability of a weighted composite. *Psychometrika*, 8, 161-168.

Examples

```
R <- matrix(c(1, .3, .3, 1), 2, 2)
fuse_reliability(c(.5, .5), R, item_reliabilities = c(.80, .85))
```

fuse_validity *Correlation of a weighted composite with an external variable*

Description

Implements the standard formula $r_{C,Y} = (w'\rho_{XY})/\sqrt{w'R_{XX}w}$ for the correlation between a weighted composite of items and an external criterion `Y`, where the items have correlations `R_XX` and individual validities `\rho_{XY}` (Lord & Novick, 1968, Ch. 4).

Usage

```
fuse_validity(weights, item_cor, item_validities)
```

Arguments

`weights`	Composite weights.
`item_cor`	Predictor (item) correlation matrix.
`item_validities`	Item-level correlations with the external variable.

Value

Scalar correlation.

Examples

```
R <- matrix(c(1, .3, .3, 1), 2, 2)
fuse_validity(c(.5, .5), R, item_validities = c(.30, .25))
```

group_tr_multivariate *Multigroup multivariate Taylor-Russell summaries*

Description

Applies `tr_multivariate()` separately by group. This is useful for sensitivity analyses in which base rates or correlation matrices differ across demographic groups. It does not by itself establish legal compliance or fairness.

Usage

```
group_tr_multivariate(
  selection_ratios,
  base_rates,
  R_list,
  group_names = NULL,
  group_proportions = NULL
)
```

Arguments

`selection_ratios`
: Vector of marginal selection ratios, common to all groups, or a list of group-specific vectors.

`base_rates`
: Numeric vector of group-specific base rates.

`R_list`
: List of group-specific correlation matrices.

`group_names`
: Optional group labels.

`group_proportions`
: Optional population proportions. If supplied, they are normalized and used to compute overall weighted summaries.

Value

A list with group-level Taylor-Russell summaries and optional weighted overall metrics.

References

De Corte, W., Lievens, F., & Sackett, P. R. (2007). Combining predictors to achieve optimal trade-offs between selection quality and adverse impact. Journal of Applied Psychology, 92, 1380-1393.

Thomas, J. G., Owen, D. B., & Gunst, R. F. (1977). Improving the use of educational tests as selection tools. Journal of Educational Statistics, 2(1), 55-77.

Examples

```
# Literature: Thomas, Owen, and Gunst (1977); De Corte et al. (2007).
R <- matrix(c(1, .30, .40, .30, 1, .35, .40, .35, 1), 3, 3)
group_tr_multivariate(c(.50, .50), base_rates = c(.50, .40),
                      R_list = list(R, R), group_names = c("A", "B"))
```

`incremental_validity` *Incremental validity for adding predictors to an existing system*

Description

Computes the difference in restricted canonical validity between a baseline predictor set and an expanded predictor set.

Usage

```
incremental_validity(
  predictor_cor,
  predictor_criterion_cor,
  criterion_cor,
  criterion_weights,
  baseline_predictors,
  added_predictors = NULL,
  focal_predictors = NULL
)
```

Arguments

`predictor_cor` Predictor correlation matrix for all candidate predictors.

`predictor_criterion_cor`
Predictor-by-criterion correlation matrix.

`criterion_cor` Criterion correlation matrix.

`criterion_weights`
Fixed criterion weights.

`baseline_predictors`
Integer indices of predictors already in the system.

`added_predictors`
Integer indices of predictors to add. Preferred name.

`focal_predictors`
Optional legacy/convenience alias for the expanded predictor set. If supplied, `added_predictors` is computed as `setdiff(focal_predictors, baseline_predictors)`. New code should use `added_predictors`.

Value

A `psu_incremental_validity` object.

References

Sturman, M. C. (2001). Utility analysis for multiple selection devices and multiple outcomes. Journal of Human Resource Costing and Accounting, 6(2), 9-28.

Examples

```
# Literature: Sturman (2001).
# Use the first call as a minimal example; the longer block illustrates
# how to interpret the function in the substantive setting discussed in the literature.
# Minimal example (Sturman (2001)).
Rxx <- matrix(c(1, .30, .20, .30, 1, .25, .20, .25, 1), 3, 3)
Rxy <- matrix(c(.30, .20, .25, .15, .10, .35), 3, 2, byrow = TRUE)
Ryy <- matrix(c(1, .40, .40, 1), 2, 2)
incremental_validity(Rxx, Rxy, Ryy, c(.6, .4), baseline_predictors = 1:2,
                     added_predictors = 3)

# Substantive example (Sturman (2001)): compare two possible additions to the same baseline.
add_2 <- incremental_validity(Rxx, Rxy, Ryy, c(.6, .4),
                              baseline_predictors = 1, added_predictors = 2)
add_3 <- incremental_validity(Rxx, Rxy, Ryy, c(.6, .4),
                              baseline_predictors = 1, added_predictors = 3)
c(add_predictor_2 = add_2$incremental_validity,
  add_predictor_3 = add_3$incremental_validity)
```

`inflation_adjusted_rate` *Combine nominal discount and inflation rates*

Description

Computes `i_a = i + f + i*f`.

Usage

```
inflation_adjusted_rate(discount_rate, inflation_rate)
```

Arguments

`discount_rate`	Real discount rate.
`inflation_rate`	Inflation rate.

Value

Inflation-adjusted discount rate.

References

Tziner, A., Meir, E. I., Dahan, M., & Birati, A. (1994). An investigation of the predictive validity and economic utility of the assessment center for the high- management level. Canadian Journal of Behavioural Science, 26, 228-245.

Holling, H. (1998). Utility analysis of personnel selection: An overview and empirical study based on objective performance measures. Methods of Psychological Research Online, 3(1), 5-24.

Examples

```
# Literature: Tziner et al. (1994); Holling (1998).
inflation_adjusted_rate(.08, .025)
```

`model_taxonomy` *Utility-analysis model taxonomy*

Description

Returns the package's working taxonomy: criterion scale crossed with selection structure. The taxonomy is designed to keep the Taylor-Russell, Brogden-Cronbach-Gleser, Sturman, Ock-Oswald, and Thomas-Owen-Gunst formulations distinct.

Usage

```
model_taxonomy()
```

Value

A data frame with model families, decision structures, and package functions.

References

Thomas, J. G., Owen, D. B., & Gunst, R. F. (1977). Improving the use of educational tests as selection tools. Journal of Educational Statistics, 2(1), 55-77.

Ock, J., & Oswald, F. L. (2018). The utility of personnel selection decisions: Comparing compensatory and multiple-hurdle selection models. Journal of Personnel Psychology, 17(4), 172-182.

Examples

```
# Literature: Thomas, Owen, and Gunst (1977); Ock and Oswald (2018).
model_taxonomy()
```

---

multiattribute_utility *Multi-attribute utility*

Description

Computes additive multi-attribute utility `sum(weights * utilities)` for one or more alternatives.

Usage

```
multiattribute_utility(values, weights, utility_functions = NULL)
```

Arguments

`values`	Numeric vector or matrix of attribute values. Alternatives are rows.
`weights`	Attribute weights. They are normalized to sum to one.
`utility_functions`	Optional list of transformation functions, one per attribute.

Value

Numeric utility score per alternative.

References

Keeney, R. L., & Raiffa, H. (1976). Decisions with multiple objectives: Preferences and value tradeoffs. Wiley.

Roth, P. L., & Bobko, P. (1997). A research agenda for multi-attribute utility analysis in human resource management. Human Resource Management Review, 7, 341-368.

Roth, P. L. (1994). Multi-attribute utility analysis using the PROMES approach. Journal of Business and Psychology, 9, 69-80.

Examples

```
# Literature: Keeney and Raiffa (1976); Roth (1994); Roth and Bobko (1997).
multiattribute_utility(matrix(c(80, .90, 70, .95), nrow = 2, byrow = TRUE),
                       weights = c(.7, .3))
```

---

multiple_hurdle_selection

Simulate conjunctive multiple-hurdle selection

Description

Simulates expected standardized criterion performance under conjunctive multiple-hurdle selection. Predictors are first in R; criterion is last. Candidates pass only if they exceed all marginal cutoffs.

Usage

```
multiple_hurdle_selection(
  selection_ratios,
  R,
  n_sim = 1e+05,
  seed = NULL,
  n_applicants = NA_real_,
  cost_per_stage = 0,
  sdy = NULL,
  applicant_n = NULL
)
```

Arguments

selection_ratios	Marginal selection ratios for each hurdle.
R	Correlation matrix for predictors and criterion, criterion last.
n_sim	Number of simulated applicants.
seed	Optional random seed.
n_applicants	Number of real applicants, used for cost calculations.
cost_per_stage	Cost per applicant at each stage. Scalar or vector.
sdy	Optional monetary value of one criterion standard deviation.
applicant_n	Legacy alias for n_applicants.

Value

A psu_comparison object.

References

Ock, J., & Oswald, F. L. (2018). The utility of personnel selection decisions: Comparing compensatory and multiple-hurdle selection models. Journal of Personnel Psychology, 17(4), 172-182.

Examples

```
# Literature: Sackett and Roth (1996); Ock and Oswald (2018).
# Minimal example (Sackett and Roth (1996); Ock and Oswald (2018)).
R <- matrix(c(1, .30, .40, .30, 1, .30, .40, .30, 1), 3, 3)
multiple_hurdle_selection(c(.50, .50), R, n_sim = 1000, seed = 1)

# Substantive example with two marginal hurdles and costs.
multiple_hurdle_selection(
  selection_ratios = c(.40, .50),
  R = R,
  n_sim = 5000,
  seed = 123,
  n_applicants = 500,
  cost_per_stage = c(100, 400),
  sdy = 60000
)
```

---

multiple_hurdle_selection_staged

Simulate staged multiple-hurdle selection with composite stages

---

Description

Simulates a sequential multiple-hurdle design in which each stage can be one predictor or a composite of predictors. This matches Ock-Oswald-style designs: an inexpensive first-stage composite can screen applicants before a later, more expensive stage such as a structured interview.

Usage

```
multiple_hurdle_selection_staged(
  stage_predictors,
  stage_selection_ratios,
  R,
  stage_weights = NULL,
  n_sim = 1e+05,
  seed = NULL,
  n_applicants = NA_real_,
  cost_per_stage = 0,
  sdy = NULL,
  applicant_n = NULL
)
```

Arguments

stage_predictors
: List of integer vectors. Each element gives the predictor columns used at that stage.

stage_selection_ratios
: Vector of within-stage selection ratios.

R
: Correlation matrix for predictors and criterion, criterion last.

stage_weights
: Optional list of weight vectors. Defaults to unit weights within each stage.

n_sim
: Number of simulated applicants.

seed
: Optional random seed.

n_applicants
: Number of real applicants, used for cost calculations.

cost_per_stage
: Cost per applicant at each stage. Scalar or vector.

sdy
: Optional monetary value of one criterion standard deviation.

applicant_n
: Legacy alias for `n_applicants`.

Value

A `psu_comparison` object.

References

Ock, J., & Oswald, F. L. (2018). The utility of personnel selection decisions: Comparing compensatory and multiple-hurdle selection models. Journal of Personnel Psychology, 17(4), 172-182.

Examples

```
# Literature: Sackett and Roth (1996); Ock and Oswald (2018).
# Use the first call as a minimal example; the longer block illustrates
# how to interpret the function in the substantive setting discussed in the literature.
# Minimal example (Sackett and Roth (1996); Ock and Oswald (2018)).
R <- diag(5)
R[lower.tri(R)] <- R[upper.tri(R)] <- .20
diag(R) <- 1
multiple_hurdle_selection_staged(list(1:3, 4), c(.25, .80), R,
                                 n_sim = 1000, seed = 1)

# Substantive example (Sackett and Roth, 1996;
# Ock and Oswald, 2018).
# Use an inexpensive first-stage composite, then an interview.
R <- matrix(c(
  1.00, .41, .04, .46, .37,
  .41, 1.00, .18, .22, .35,
  .04, .18, 1.00, .66, .16,
  .46, .22, .66, 1.00, .23,
  .37, .35, .16, .23, 1.00
), 5, 5, byrow = TRUE)
multiple_hurdle_selection_staged(
  stage_predictors = list(c(1, 3, 4), 2),
```

```
    stage_selection_ratios = c(.25, .80),
    R = R,
    n_sim = 5000,
    seed = 123,
    n_applicants = 500,
    cost_per_stage = c(100, 900),
    sdy = 60000
  )
```

---

naylor_shine *Naylor-Shine expected criterion gain*

Description

Computes expected standardized criterion gain among selected applicants and, optionally, converts it to utility using sdy, n_selected, tenure, and cost. The expected standardized criterion gain is validity * selected_mean_z(selection_ratio).

Usage

```
naylor_shine(
  validity,
  selection_ratio,
  sdy = 1,
  n_selected = 1,
  tenure = 1,
  cost = 0
)
```

Arguments

validity	Predictor-criterion validity, usually denoted r_xy.
selection_ratio	Selection ratio, usually denoted SR.
sdy	Standard deviation of job performance in monetary or criterion units.
n_selected	Number of selected applicants.
tenure	Expected tenure or number of periods.
cost	Total cost.

Value

A psu_ns object.

References

Naylor, J. C., & Shine, L. C. (1965). A table for determining the increase in mean criterion score obtained by using a selection device. Journal of Industrial Psychology, 3, 33-42.

Examples

```
# Literature: Naylor and Shine (1965).
# Use the first call as a minimal example; the longer block illustrates
# how to interpret the function in the substantive setting discussed in the literature.
# Minimal example: standardized criterion gain only.
naylor_shine(validity = .35, selection_ratio = .20)

# Substantive example (Naylor and Shine (1965)): standardized gain translated to monetary utility.
naylor_shine(
  validity = .35,
  selection_ratio = .20,
  sdy = 50000,
  n_selected = 100,
  tenure = 3,
  cost = 75000
)
```

---

offer_rejection_adjustment
Offer-rejection adjustment for selection utility (Murphy, 1986)

Description

Adjusts the expected standardized criterion score of accepted hires when offer recipients can decline. When the probability of accepting an offer is *negatively* correlated with candidate quality (top candidates have more outside options), the realized mean criterion of accepted hires is below the mean of selected (offered) candidates.

Usage

```
offer_rejection_adjustment(
  expected_z_offered,
  mode = c("uniform", "selective", "correlated"),
  acceptance_rate = 1,
  rho_quality_acceptance = 0,
  logit_intercept = NULL,
  logit_slope = NULL,
  n_offered = NULL
)
```

Arguments

`expected_z_offered`
: Expected standardized score of offered candidates (e.g., `selected_mean_z(selection_ratio)`).

`mode`
: One of `"uniform"`, `"selective"`, or `"correlated"`.

`acceptance_rate`
: Expected proportion of offers accepted (used in all three modes for the headcount-scaling output).

rho_quality_acceptance
: Correlation between standardized candidate quality and acceptance propensity (used for mode = "correlated"). Negative values reflect adverse selection (top candidates more likely to decline).

logit_intercept, logit_slope
: Logit link coefficients for mode = "selective". The slope is typically negative for adverse selection.

n_offered
: Optional integer; if supplied, the function also returns the expected number of accepted hires.

Details

Three modes are supported:

- mode = "uniform": a fixed acceptance probability p independent of candidate quality. The expected criterion of accepted hires equals the expected criterion of those offered, but the realized headcount is scaled by p.
- mode = "selective": the probability of acceptance depends on candidate standardized quality z through a logit link logit(p) = a + b * z with b < 0 for adverse selection. The adjusted mean criterion is computed by integrating the standard normal weighted by the acceptance probability.
- mode = "correlated": a closed-form approximation under the assumption that quality and acceptance are jointly normal with correlation rho_quality_acceptance. The adjustment is $\bar{z}_{accepted} \approx \bar{z}_{offered} + \rho \cdot (\lambda(z_p) - \bar{z}_{offered})$ for an acceptance threshold z_p derived from the expected acceptance rate.

Value

A list with expected_z_accepted, acceptance_rate, effective_validity_loss (the difference between offered and accepted means), and optionally expected_n_accepted.

References

Hogarth, R. M., & Einhorn, H. J. (1976). Optimal strategies for personnel selection when candidates can reject job offers. *Journal of Business*, 49, 479-495.

Murphy, K. R. (1986). When your top choice turns you down: Effect of rejected offers on the utility of selection tests. *Psychological Bulletin*, 99, 133-138.

Examples

```
z_offered <- selected_mean_z(0.20)

# Uniform 70% acceptance rate, no quality dependence:
offer_rejection_adjustment(z_offered, mode = "uniform",
                           acceptance_rate = 0.70, n_offered = 100)

# Adverse selection: top candidates more likely to decline.
offer_rejection_adjustment(z_offered, mode = "correlated",
                           acceptance_rate = 0.70,
```

```
rho_quality_acceptance = -0.20,
n_offered = 100)
```

pareto_frontier *Pareto frontier indicator*

Description

Identifies non-dominated alternatives for objectives to be maximized or minimized.

Usage

```
pareto_frontier(objectives, maximize = TRUE)
```

Arguments

objectives	Numeric matrix/data frame. Alternatives are rows, objectives columns.
maximize	Logical vector indicating whether each objective is to be maximized. Scalar values are recycled.

Value

Logical vector indicating Pareto-efficient rows.

References

De Corte, W., Lievens, F., & Sackett, P. R. (2007). Combining predictors to achieve optimal trade-offs between selection quality and adverse impact. Journal of Applied Psychology, 92, 1380-1393.
De Corte, W., Sackett, P. R., & Lievens, F. (2011). Designing Pareto-optimal selection systems: Formalizing the decisions required for selection system development. Journal of Applied Psychology, 96, 907-926.

Examples

```
# Literature: De Corte, Lievens, and Sackett (2007); De Corte, Sackett, and Lievens (2011).
pareto_frontier(data.frame(validity = c(.30, .35, .32), diversity = c(.80, .70, .85)))
```

probation_adjustment — *Expected standardized performance after a probation cutoff*

Description

Computes the mean of a standard normal criterion among employees surviving a probation rule `Y >= probation_cutoff_z`.

Usage

```
probation_adjustment(probation_cutoff_z)
```

Arguments

`probation_cutoff_z`
Probation cutoff on the standardized criterion.

Value

Expected standardized criterion score among survivors.

References

De Corte, W. (1994). Utility analysis for the one-cohort selection-retention decision with a probationary period. Journal of Applied Psychology, 79, 402-411.

Sturman, M. C. (2001). Utility analysis for multiple selection devices and multiple outcomes. Journal of Human Resource Costing and Accounting, 6(2), 9-28.

Examples

```
# Literature: De Corte (1994); Sturman (2001).
probation_adjustment(-1)
```

probation_utility — *Utility with a probation-period survivor adjustment*

Description

A compact helper for selection systems where year 1 utility follows BCG and later periods include an additional survivor-performance gain caused by a probation cutoff.

Usage

```
probation_utility(
  validity,
  selection_ratio,
  sdy,
  n_selected,
  tenure,
  probation_cutoff_z,
  cost = 0
)
```

Arguments

validity	Predictor-criterion validity.
selection_ratio	Selection ratio.
sdy	Standard deviation of job performance in monetary units.
n_selected	Number of selected applicants in period 1.
tenure	Total number of periods.
probation_cutoff_z	Standardized criterion cutoff used after probation.
cost	Total cost.

Value

A psu_bcg object.

References

De Corte, W. (1994). Utility analysis for the one-cohort selection-retention decision with a probationary period. Journal of Applied Psychology, 79, 402-411.

Sturman, M. C. (2001). Utility analysis for multiple selection devices and multiple outcomes. Journal of Human Resource Costing and Accounting, 6(2), 9-28.

Examples

```
# Literature: De Corte (1994); Sturman (2001).
probation_utility(.35, .20, 50000, 100, tenure = 3, probation_cutoff_z = -1)
```

relative_weights *Johnson relative weights for one criterion*

Description

Computes approximate relative weights for correlated predictors in a multiple regression with one criterion.

Usage

```
relative_weights(predictor_cor, criterion_cor)
```

Arguments

predictor_cor	Predictor correlation matrix.
criterion_cor	Vector of predictor-criterion correlations.

Value

A data frame with raw and rescaled relative weights.

References

Johnson, J. W. (2000). A heuristic method for estimating the relative weight of predictor variables in multiple regression. Multivariate Behavioral Research, 35, 1-19.

Examples

```
# Literature: Johnson (2000).
relative_weights(matrix(c(1, .30, .30, 1), 2, 2), c(.40, .30))
```

restricted_canonical_validity *Restricted canonical validity for a fixed criterion composite*

Description

Computes Sturman-style restricted canonical validity. Predictor weights are optimized, but criterion weights are fixed by the analyst.

Usage

```
restricted_canonical_validity(
  predictor_cor,
  predictor_criterion_cor,
  criterion_cor,
  criterion_weights
)
```

Arguments

`predictor_cor` Predictor correlation matrix, `Sigma_11`.

`predictor_criterion_cor`
Matrix of predictor-criterion correlations, `Sigma_12`, with predictors in rows and criteria in columns.

`criterion_cor` Criterion correlation matrix, `Sigma_22`.

`criterion_weights`
Fixed criterion weights, `b`.

Value

A `psu_incremental_validity` object with restricted canonical validity and optimized standardized predictor weights.

References

Sturman, M. C. (2001). Utility analysis for multiple selection devices and multiple outcomes. Journal of Human Resource Costing and Accounting, 6(2), 9-28.

Examples

```
# Literature: Sturman (2001).
# Use the first call as a minimal example; the longer block illustrates
# how to interpret the function in the substantive setting discussed in the literature.
# Minimal example (Sturman (2001)).
S11 <- matrix(c(1, .30, .30, 1), 2, 2)
S12 <- matrix(c(.30, .20, .25, .15), 2, 2)
S22 <- matrix(c(1, .40, .40, 1), 2, 2)
restricted_canonical_validity(S11, S12, S22, criterion_weights = c(.6, .4))

# Substantive example (Sturman (2001)): change criterion weights and compare restricted validity.
task_weighted <- restricted_canonical_validity(S11, S12, S22, c(.8, .2))
balanced <- restricted_canonical_validity(S11, S12, S22, c(.5, .5))
c(task_weighted = task_weighted$validity, balanced = balanced$validity)
```

`risk_adjusted_utility` *Risk-adjusted utility*

Description

Computes a mean-variance risk-adjusted utility score. With `risk_aversion = 0`, the score equals expected utility. Larger values penalize uncertainty more strongly.

Usage

```
risk_adjusted_utility(expected_utility, utility_sd, risk_aversion = 0)
```

Arguments

`expected_utility`
: Expected utility or mean posterior/simulation utility.

`utility_sd`
: Standard deviation of utility.

`risk_aversion`
: Non-negative risk-aversion parameter.

Value

Risk-adjusted utility score.

References

Bhattacharya, M., & Wright, P. M. (2005). Managing human assets in an uncertain world: Applying real options theory to HRM. International Journal of Human Resource Management, 16, 929-948.

Cronshaw, S. F., Alexander, R. A., Wiesner, W. H., & Barrick, M. R. (1987). Incorporating risk into selection utility. Organizational Behavior and Human Decision Processes, 40, 270-286.

Examples

```
# Literature: Cronshaw et al. (1987); Bhattacharya and Wright (2005).
risk_adjusted_utility(expected_utility = 100000, utility_sd = 25000,
                      risk_aversion = 1e-6)
```

`sdy_cost_accounting` *SDy from cost-accounting data*

Description

Computes individual criterion values from production units and unit values, then returns the standard deviation of those values.

Usage

```
sdy_cost_accounting(units, unit_values, na.rm = TRUE)
```

Arguments

`units`
: Numeric matrix or data frame. Rows are employees; columns are production units, activities, or outputs.

`unit_values`
: Numeric vector of monetary values per unit. Length one or one value per column of `units`.

`na.rm`
: Should missing values be removed in the SD calculation?

Value

A list with individual criterion values and `sdy`.

References

Cronbach, L. J., & Gleser, G. C. (1965). Psychological tests and personnel decisions (2nd ed.). University of Illinois Press.

Holling, H. (1998). Utility analysis of personnel selection: An overview and empirical study based on objective performance measures. Methods of Psychological Research Online, 3(1), 5-24.

Cascio, W. F. (1982). Costing human resources: The financial impact of behavior in organizations. Kent.

Examples

```
# Literature: Cronbach and Gleser (1965); Cascio (1982); Holling (1998).
sdy_cost_accounting(matrix(c(10, 12, 8, 11), ncol = 2), unit_values = c(100, 200))
```

---

sdy_crepid — *SDy from a simplified CREPID-style activity decomposition*

Description

Computes a monetary performance index by weighting activity ratings with activity time/frequency and importance weights.

Usage

```
sdy_crepid(
  activities,
  ratings,
  salary,
  time_col = "time_frequency",
  importance_col = "importance",
  activity_names = NULL,
  na.rm = TRUE
)
```

Arguments

`activities`	Data frame with activity-level metadata.
`ratings`	Numeric matrix/data frame. Rows are employees, columns are activities.
`salary`	Average salary or criterion value to distribute across activities.
`time_col`	Name of the time/frequency column in `activities`.
`importance_col`	Name of the importance column in `activities`.
`activity_names`	Optional activity labels.
`na.rm`	Should missing values be removed in the SD calculation?

Value

A list with activity weights, individual criterion values, and sdy.

References

Cascio, W. F., & Ramos, R. A. (1986). Development and application of a new method for assessing job performance in behavioral/economic terms. Journal of Applied Psychology, 71, 20-28.

Examples

```
# Literature: Cascio and Ramos (1986).
activities <- data.frame(time_frequency = c(.4, .6), importance = c(2, 3))
ratings <- matrix(c(3, 4, 2, 5, 4, 4), ncol = 2, byrow = TRUE)
sdy_crepid(activities, ratings, salary = 80000)
```

---

sdy_observed *Observed SDy from monetary criterion data*

Description

Computes the observed standard deviation of job performance in monetary or productivity units. This is the direct empirical counterpart to subjective SDy estimation methods.

Usage

```
sdy_observed(y, na.rm = TRUE)
```

Arguments

y	Numeric vector of monetary or productivity criterion values.
na.rm	Should missing values be removed?

Value

Observed SDy.

References

Holling, H. (1998). Utility analysis of personnel selection: An overview and empirical study based on objective performance measures. Methods of Psychological Research Online, 3(1), 5-24.

Examples

```
# Literature: Holling (1998).
sdy_observed(c(100, 120, 80, 150))
```

sdy_percentile *Estimate SDy from percentile judgments*

Description

Implements the percentile approximation `SDy = (P85 - P15) / 2`.

Usage

```
sdy_percentile(p15, p85)
```

Arguments

p15	Estimated monetary value of performance at the 15th percentile.
p85	Estimated monetary value of performance at the 85th percentile.

Value

Estimated standard deviation of job performance in monetary units.

References

Bobko, P., Karren, R., & Parkington, J. J. (1983). Estimation of standard deviations in utility analyses: An empirical test. Journal of Applied Psychology, 68, 170-176.

Schmidt, F. L., Hunter, J. E., McKenzie, R. C., & Muldrow, T. W. (1979). Impact of valid selection procedures on work-force productivity. Journal of Applied Psychology, 64, 609-626.

Examples

```
# Literature: Schmidt et al. (1979); Bobko, Karren, and Parkington (1983).
sdy_percentile(p15 = 60000, p85 = 140000)
```

sdy_proportional *Estimate SDy with proportional rules*

Description

Computes a salary- or value-based SDy estimate using a multiplier such as .40 or .70.

Usage

```
sdy_proportional(mean_pay, multiplier = 0.4)
```

Arguments

`mean_pay` Mean pay or mean output value.

`multiplier` Proportional SDy multiplier. Defaults to `.40`.

Value

Estimated SDy.

References

Schmidt, F. L., Hunter, J. E., & Pearlman, K. (1982). Assessing the economic impact of personnel programs on workforce productivity. Personnel Psychology, 35, 333-347.

Hunter, J. E., & Schmidt, F. L. (1982). Fitting people to jobs: The impact of personnel selection on national productivity. In M. D. Dunnette & E. A. Fleishman (Eds.), Human performance and productivity (Vol. 1, pp. 233-284). Erlbaum.

Examples

```
# Literature: Schmidt, Hunter, and Pearlman (1982); Hunter and Schmidt (1982).
sdy_proportional(mean_pay = 80000, multiplier = .40)
sdy_proportional(mean_pay = 80000, multiplier = .70)
```

---

sdy_rbn *Estimate SDy with a coefficient-of-variation approach*

Description

A compact implementation of the Raju-Burke-Normand logic: `SDy = CV * mean_pay`. Use this function when the coefficient of variation is theoretically or empirically justified for the job family.

Usage

```
sdy_rbn(mean_pay, coefficient_variation)
```

Arguments

`mean_pay` Mean pay or mean criterion value.

`coefficient_variation`
Coefficient of variation for job performance value.

Value

Estimated SDy.

References

Raju, N. S., Burke, M. J., & Normand, J. (1990). A new approach for utility analysis. Journal of Applied Psychology, 75, 3-12.

Examples

```
# Literature: Raju, Burke, and Normand (1990).
sdy_rbn(mean_pay = 80000, coefficient_variation = .35)
```

`sdy_superior_equivalents` *SDy from superior-equivalents judgments*

Description

Computes SDy from a judged monetary difference between a superior and a typical performer, divided by the standardized distance assumed to separate them.

Usage

```
sdy_superior_equivalents(superior_value, typical_value, z_difference = 1)
```

Arguments

`superior_value`	Monetary value of the superior performer.
`typical_value`	Monetary value of the typical performer.
`z_difference`	Standardized distance between the two performers. Defaults to 1, but can be set to another value if the judgment anchors imply it.

Value

Estimated SDy.

References

Eaton, N. K., Wing, H., & Mitchell, K. J. (1985). Alternate methods of estimating the dollar value of performance. Personnel Psychology, 38, 27-40.

Burke, M. J., & Frederick, J. T. (1984). Two modified procedures for estimating standard deviations in utility analyses. Journal of Applied Psychology, 69, 482-489.

Burke, M. J., & Frederick, J. T. (1986). A comparison of economic utility estimates for alternative SDy estimation procedures. Journal of Applied Psychology, 71, 334-339.

Examples

```
# Literature: Eaton, Wing, and Mitchell (1985); Burke and Frederick (1984, 1986).
sdy_superior_equivalents(superior_value = 140000, typical_value = 100000)
```

`selected_mean_z` *Expected standardized predictor score among selected applicants*

Description

Computes the mean of a standard normal predictor after top-down selection at a given selection ratio: `dnorm(qnorm(1 - selection_ratio)) / selection_ratio`.

Usage

```
selected_mean_z(selection_ratio)
```

Arguments

`selection_ratio`
: Proportion of applicants selected. Must be in `(0, 1)`.

Value

Numeric vector with expected standardized predictor scores.

References

Naylor, J. C., & Shine, L. C. (1965). A table for determining the increase in mean criterion score obtained by using a selection device. Journal of Industrial Psychology, 3, 33-42.

Examples

```
# Literature: Naylor and Shine (1965).
selected_mean_z(c(.10, .20, .50))
```

`selection_table` *Selection table and classification metrics*

Description

Computes a 2x2 classification table from observed selected/success outcomes.

Usage

```
selection_table(selected, success)
```

Arguments

`selected`	Logical or 0/1 vector indicating selection.
`success`	Logical or 0/1 vector indicating criterion success.

Value

A list with table and classification metrics.

References

Thomas, J. G., Owen, D. B., & Gunst, R. F. (1977). Improving the use of educational tests as selection tools. Journal of Educational Statistics, 2(1), 55-77.

Taylor, H. C., & Russell, J. T. (1939). The relationship of validity coefficients to the practical effectiveness of tests in selection. Journal of Applied Psychology, 23, 565-578.

Examples

```
# Literature: Taylor and Russell (1939); Thomas, Owen, and Gunst (1977).
selection_table(c(1, 1, 0, 0), c(1, 0, 1, 0))
```

---

selection_utility_from_z

Selection utility from expected standardized criterion performance

---

Description

Computes the Ock-Oswald/BCG-style utility expression `expected_criterion_z * sdy * n_selected - n_applicants * cost_per_applicant - fixed_cost` from an expected standardized criterion score among selected applicants.

Usage

```
selection_utility_from_z(
  expected_criterion_z,
  sdy,
  n_selected,
  n_applicants = n_selected,
  cost_per_applicant = 0,
  fixed_cost = 0,
  applicant_n = NULL
)
```

Arguments

`expected_criterion_z`	Expected criterion performance in standard deviation units.
`sdy`	Monetary value of one criterion standard deviation.
`n_selected`	Number of selected applicants.
`n_applicants`	Number of applicants assessed. This is the preferred name in v0.4.0.
`cost_per_applicant`	Cost per applicant assessed.
`fixed_cost`	Additional fixed cost.
`applicant_n`	Legacy alias for `n_applicants`. Use `n_applicants` in new code.

Value

A psu_comparison object.

References

Cronbach, L. J., & Gleser, G. C. (1965). Psychological tests and personnel decisions (2nd ed.). University of Illinois Press.

Naylor, J. C., & Shine, L. C. (1965). A table for determining the increase in mean criterion score obtained by using a selection device. Journal of Industrial Psychology, 3, 33-42.

Brogden, H. E. (1946). On the interpretation of the correlation coefficient as a measure of predictive efficiency. Journal of Educational Psychology, 37, 65-76.

Examples

```
# Literature: Naylor and Shine (1965); Brogden (1946); Cronbach and Gleser (1965).
# Minimal example: expected performance converted to monetary utility.
selection_utility_from_z(1.25, sdy = 50000, n_selected = 20,
                         n_applicants = 100, cost_per_applicant = 200)

# Substantive example: compare two systems from expected criterion gains.
compensatory <- selection_utility_from_z(1.25, 50000, n_selected = 20,
                                         n_applicants = 100,
                                         cost_per_applicant = 1000)
hurdle <- selection_utility_from_z(.55, 50000, n_selected = 20,
                                   n_applicants = 100,
                                   cost_per_applicant = 300)
compensatory$net_utility - hurdle$net_utility
```

---

sensitivity_grid *Sensitivity grid for BCG utility*

Description

Computes BCG net utility for all combinations of selected parameter values.

Usage

```
sensitivity_grid(validity, selection_ratio, sdy, n_selected, tenure, cost = 0)
```

Arguments

validity	Numeric vector of validities.
selection_ratio	Numeric vector of selection ratios.
sdy	Numeric vector of SDy values.
n_selected	Number selected.
tenure	Expected tenure.
cost	Cost.

Value

A data frame with one row per scenario.

References

Cronshaw, S. F., Alexander, R. A., Wiesner, W. H., & Barrick, M. R. (1987). Incorporating risk into selection utility. Organizational Behavior and Human Decision Processes, 40, 270-286.

Ock, J., & Oswald, F. L. (2018). The utility of personnel selection decisions: Comparing compensatory and multiple-hurdle selection models. Journal of Personnel Psychology, 17(4), 172-182.

Boudreau, J. W. (1991). Utility analysis for decisions in human resource management. In M. D. Dunnette & L. M. Hough (Eds.), Handbook of industrial and organizational psychology (Vol. 2, pp. 621-745). Consulting Psychologists Press.

Examples

```
# Literature: Cronshaw et al. (1987); Boudreau (1991); Ock and Oswald (2018).
# Use the first call as a minimal example; the longer block illustrates
# how to interpret the function in the substantive setting discussed in the literature.
# Minimal example (Cronshaw et al. (1987); Boudreau (1991); Ock and Oswald (2018)).
sensitivity_grid(validity = c(.20, .30), selection_ratio = c(.10, .20),
                 sdy = c(40000, 60000), n_selected = 100, tenure = 3)

# Substantive example (Cronshaw et al., 1987; Boudreau, 1991;
# Ock and Oswald, 2018). Find the best sensitivity scenario.
grid <- sensitivity_grid(validity = seq(.20, .40, .10),
                         selection_ratio = c(.10, .20, .40),
                         sdy = c(30000, 60000),
                         n_selected = 100, tenure = 3, cost = 75000)
grid[which.max(grid$net_utility), ]
```

---

shp_utility *Schmidt-Hunter-Pearlman intervention utility*

Description

Computes utility from an intervention effect size rather than from a selection validity coefficient. This is appropriate for training or intervention designs where the key input is a standardized mean difference.

Usage

```
shp_utility(effect_size_d, sdy, n_treated, tenure, cost = 0)
```

Arguments

effect_size_d	Standardized mean difference caused by the intervention.
sdy	Standard deviation of job performance in monetary units.
n_treated	Number of employees receiving the intervention.
tenure	Expected duration of the effect in periods.
cost	Total intervention cost.

Value

A psu_shp object.

References

Schmidt, F. L., Hunter, J. E., & Pearlman, K. (1982). Assessing the economic impact of personnel programs on workforce productivity. Personnel Psychology, 35, 333-347.

Cohen, J. (1988). Statistical power analysis for the behavioral sciences (2nd ed.). Erlbaum.

Examples

```
# Literature: Schmidt, Hunter, and Pearlman (1982); Cohen (1988).
# Use the first call as a minimal example; the longer block illustrates
# how to interpret the function in the substantive setting discussed in the literature.
# Minimal example (Schmidt, Hunter, and Pearlman (1982); Cohen (1988)).
shp_utility(effect_size_d = .30, sdy = 50000, n_treated = 100,
            tenure = 2, cost = 40000)

# Substantive example (Schmidt, Hunter, and Pearlman, 1982;
# Cohen, 1988). Compare two training designs.
short_training <- shp_utility(.20, 50000, n_treated = 120, tenure = 1, cost = 30000)
intensive_training <- shp_utility(.35, 50000, n_treated = 120, tenure = 1,
                                  cost = 95000)
c(short = short_training$net_utility, intensive = intensive_training$net_utility)
```

---

sturman_comprehensive *Sturman's (2001) comprehensive utility analysis*

Description

Composes the six adjustments of Sturman's (2001) comprehensive model (§15 of the package's accompanying review) into a single call. The returned object includes both the integrated comprehensive estimate and a stepwise cascade that documents the contribution of each adjustment.

Usage

```
sturman_comprehensive(
  validity,
  baseline_validity = 0,
  selection_ratio,
  sdy,
  n_year_one,
  tenure = 5,
  fixed_cost = 0,
  hires_per_period = NULL,
  losses_per_period = NULL,
  tax_rate = 0,
  discount_rate = 0,
  variable_value = 0,
  maintenance_cost_per_period = NULL,
  predictor_cor = NULL,
  predictor_criterion_cor = NULL,
  criterion_cor = NULL,
  criterion_weights = NULL,
  probation_cutoff_z = NULL,
  acceptance_rate = 1,
  quality_acceptance_correlation = 0
)
```

Arguments

`validity` Focal-system validity (used directly when `predictor_cor` is `NULL`; replaced by the restricted canonical validity otherwise).

`baseline_validity`
Operating-system baseline validity. Default 0 collapses to a random-baseline analysis, which the function will warn about.

`selection_ratio`
Selection ratio.

`sdy` Standard deviation of job performance in monetary units.

`n_year_one` Number of hires in year 1.

`tenure` Horizon in years (>= 1).

`fixed_cost` Year-1 selection cost (currency).

`hires_per_period`, `losses_per_period`
Optional vectors of length `tenure` for replacement hires and turnover losses; if `NULL` a steady state with `n_year_one` per year is used.

`tax_rate`, `discount_rate`, `variable_value`
Boudreau parameters.

`maintenance_cost_per_period`
Optional cost vector of length `tenure`.

predictor_cor, predictor_criterion_cor, criterion_cor, criterion_weights
: If supplied, the function computes the restricted canonical validity from this multidimensional criterion specification and substitutes it for validity.

probation_cutoff_z
: Standardized cutoff for the probation rule (default NULL skips this adjustment).

acceptance_rate, quality_acceptance_correlation
: Murphy's (1986) offer-rejection adjustment. If acceptance_rate < 1, the function adjusts the year-1 expected criterion mean and headcount accordingly.

Details

The six adjustments combined here are: (1) baseline correction (Sturman, 2000, 2001), (2) restricted canonical validity for a multidimensional criterion, (3) multi-period employee flows, (4) Boudreau-style economic adjustments (taxes, variable costs, discount rate), (5) De Corte (1994) probation-period truncation, and optionally (6) Murphy's (1986) offer-rejection adjustment. See bcg_utility(), boudreau_utility(), restricted_canonical_validity(), probation_adjustment(), employee_flow(), and offer_rejection_adjustment() for the underlying components.

Value

Object of class c("psu_sturman", "psu_utility") with components: net_utility (final comprehensive estimate), cascade (a data frame documenting each step), effective_validity, effective_baseline_validi and the relevant intermediate objects.

References

De Corte, W. (1994). Utility analysis for the one-cohort selection-retention decision with a probationary period. *Journal of Applied Psychology*, 79, 402-411.

Murphy, K. R. (1986). When your top choice turns you down: Effect of rejected offers on the utility of selection tests. *Psychological Bulletin*, 99, 133-138.

Sturman, M. C. (2000). Implications of utility analysis adjustments for estimates of human resource intervention value. *Journal of Management*, 26, 281-299.

Sturman, M. C. (2001). Utility analysis for multiple selection devices and multiple outcomes. *Journal of Human Resource Costing and Accounting*, 6(2), 9-28.

Examples

```
Rxx <- matrix(c(1, .30, .30, 1), 2, 2)
Rxy <- matrix(c(.30, .10, .15, .25), 2, 2, byrow = TRUE)
Ryy <- matrix(c(1, .40, .40, 1), 2, 2)

sturman_comprehensive(
  validity = .35, baseline_validity = .20, selection_ratio = .20,
  sdy = 50000, n_year_one = 100, tenure = 5, fixed_cost = 75000,
  tax_rate = .25, discount_rate = .08,
  predictor_cor = Rxx, predictor_criterion_cor = Rxy,
  criterion_cor = Ryy, criterion_weights = c(.7, .3),
  probation_cutoff_z = -1,
```

```
  acceptance_rate = 0.70, quality_acceptance_correlation = -0.20
)
```

---

tr_binomial_success_probability

Binomial sampling probabilities for Taylor-Russell success rates

---

Description

Converts a Taylor-Russell success ratio into finite-sample probabilities. This follows the finite-sampling logic discussed by Thomas, Owen, and Gunst: once a conditional probability of success is known, the number of successful selected applicants in a finite cohort can be modeled with a binomial distribution.

Usage

```
tr_binomial_success_probability(n_selected, ppv, at_least = NULL)
```

Arguments

n_selected	Number of selected applicants.
ppv	Positive predictive value / success ratio among selected applicants.
at_least	Optional threshold for computing P(successes >= at_least).

Value

A data frame with the full binomial distribution and, if requested, the cumulative upper-tail probability.

References

Thomas, J. G., Owen, D. B., & Gunst, R. F. (1977). Improving the use of educational tests as selection tools. Journal of Educational Statistics, 2(1), 55-77.

Examples

```
# Literature: Thomas, Owen, and Gunst (1977).
tr_binomial_success_probability(n_selected = 20, ppv = .91, at_least = 18)
```

tr_classic *Taylor-Russell utility for one predictor*

Description

Computes the Taylor-Russell classification table for one normally distributed predictor and one dichotomized criterion.

Usage

```
tr_classic(base_rate, selection_ratio, validity, digits = 3)
```

Arguments

base_rate	Population proportion of successful applicants, `P(Y >= y_c)`.
selection_ratio	Proportion selected, `P(X >= x_c)`.
validity	Predictor-criterion correlation.
digits	Number of digits used for printed summaries.

Value

A list with thresholds, TP, FP, FN, TN, PPV, sensitivity, specificity, and incremental success over the base rate.

References

Taylor, H. C., & Russell, J. T. (1939). The relationship of validity coefficients to the practical effectiveness of tests in selection. Journal of Applied Psychology, 23, 565-578.

Cascio, W. F. (1980). Responding to the demand for accountability: A critical analysis of three utility models. Organizational Behavior and Human Performance, 25, 32-45.

Examples

```
# Literature: Taylor and Russell (1939); Cascio (1980).
# Use the first call as a minimal example; the longer block illustrates
# how to interpret the function in the substantive setting discussed in the literature.
# Minimal example (Taylor and Russell (1939); Cascio (1980)).
tr_classic(base_rate = .50, selection_ratio = .20, validity = .35)

# Substantive example (Taylor and Russell, 1939; Cascio, 1980).
# Examine how selectivity changes the success ratio.
low_sr <- tr_classic(base_rate = .50, selection_ratio = .10, validity = .35)
high_sr <- tr_classic(base_rate = .50, selection_ratio = .50, validity = .35)
c(low_selection_ratio = low_sr$ppv, high_selection_ratio = high_sr$ppv)
```

tr_multivariate — *Multivariate Taylor-Russell utility for conjunctive multiple-hurdle selection*

Description

Implements the Thomas-Owen-Gunst multivariate extension of the Taylor-Russell model. Candidates are selected if and only if they exceed all predictor cutoffs. The correlation matrix must include the predictors first and the criterion last.

Usage

```
tr_multivariate(selection_ratios, base_rate, R, digits = 3)
```

Arguments

`selection_ratios`	Vector of marginal selection ratios, one per predictor.
`base_rate`	Population proportion of successful applicants.
`R`	Correlation matrix of dimension `(k + 1) x (k + 1)`. Predictors must occupy the first k rows/columns; the criterion must be last.
`digits`	Number of digits used for printed summaries.

Value

A `psu_tr` object with TP, FP, FN, TN, joint selection ratio, PPV, sensitivity, specificity, and cutoffs.

References

Thomas, J. G., Owen, D. B., & Gunst, R. F. (1977). Improving the use of educational tests as selection tools. Journal of Educational Statistics, 2(1), 55-77.

Taylor, H. C., & Russell, J. T. (1939). The relationship of validity coefficients to the practical effectiveness of tests in selection. Journal of Applied Psychology, 23, 565-578.

Genz, A., & Bretz, F. (2009). Computation of multivariate normal and t probabilities. Springer.

Examples

```
# Literature: Taylor and Russell (1939); Thomas, Owen, and Gunst
# (1977); Genz and Bretz (2009).
# Use the first call as a minimal example; the longer block illustrates
# how to interpret the function in the substantive setting discussed in the literature.
# Minimal example (Taylor and Russell, 1939;
# Thomas, Owen, and Gunst, 1977; Genz and Bretz, 2009).
R <- matrix(c(1, .30, .40,
              .30, 1, .35,
              .40, .35, 1), nrow = 3, byrow = TRUE)
tr_multivariate(selection_ratios = c(.50, .50), base_rate = .50, R = R)
```

```
# Substantive example (Taylor and Russell, 1939;
# Thomas, Owen, and Gunst, 1977; Genz and Bretz, 2009).
# Compare two validity patterns under the same marginal cutoffs.
R_stronger <- matrix(c(1, .30, .60,
                       .30, 1, .55,
                       .60, .55, 1), nrow = 3, byrow = TRUE)
weak <- tr_multivariate(c(.50, .50), base_rate = .50, R = R)
strong <- tr_multivariate(c(.50, .50), base_rate = .50, R = R_stronger)
c(weak_ppv = weak$ppv, strong_ppv = strong$ppv)
```

---

tr_multivariate_equal_cutoff

Solve equal marginal cutoffs for a target joint selection ratio

---

Description

Thomas, Owen, and Gunst's printed tables are indexed by the overall proportion selected under two equal cutoffs. This helper solves the common marginal selection ratio that yields a target conjunctive selection ratio for any predictor correlation matrix, then calls `tr_multivariate()`.

Usage

```
tr_multivariate_equal_cutoff(
  joint_selection_ratio,
  base_rate,
  R,
  interval = NULL,
  tol = 1e-08,
  digits = 3
)
```

Arguments

`joint_selection_ratio`	Target conjunctive selection ratio, `P(X_1 >= c, ..., X_k >= c)`.
`base_rate`	Population proportion of successful applicants.
`R`	Correlation matrix with predictors first and criterion last.
`interval`	Optional search interval for the common marginal selection ratio. Defaults to `(joint_selection_ratio, 1)`.
`tol`	Numerical tolerance passed to `optimize()`.
`digits`	Number of digits used for printed summaries.

Value

A `psu_tr` object from `tr_multivariate()` with the solved marginal selection ratio, the target joint selection ratio, the computed joint selection ratio, and the numerical joint-selection error added.

References

Thomas, J. G., Owen, D. B., & Gunst, R. F. (1977). Improving the use of educational tests as selection tools. Journal of Educational Statistics, 2(1), 55-77.

Waller, N. G. (2024). TaylorRussell: A Taylor-Russell function for multiple predictors (R package version 1.2.1). CRAN.

Examples

```
# Literature: Thomas, Owen, and Gunst (1977); Waller (2024).
# Use the first call as a minimal example; the longer block illustrates
# how to interpret the function in the substantive setting discussed in the literature.
# Minimal example (Thomas, Owen, and Gunst (1977); Waller (2024)).
R <- matrix(c(1, .50, .70,
              .50, 1, .70,
              .70, .70, 1), 3, 3, byrow = TRUE)
tr_multivariate_equal_cutoff(joint_selection_ratio = .20, base_rate = .60, R = R)

# Substantive example (Thomas, Owen, and Gunst, 1977;
# Waller, 2024). Reproduce the Example 1 pattern.
tog <- tr_multivariate_equal_cutoff(.20, .60, R)
c(marginal_sr = tog$solved_marginal_selection_ratio, ppv = tog$ppv)
```

---

tr_solve *Solve one Taylor-Russell parameter from the other three*

Description

Solves for one missing Taylor-Russell parameter among base rate, selection ratio, validity, and PPV. Exactly one of the four arguments must be `NULL`. The default validity interval is non-negative to match the classical Taylor-Russell table convention and the defensive behavior of the `TaylorRussell::TR()` implementation.

Usage

```
tr_solve(
  base_rate = NULL,
  selection_ratio = NULL,
  validity = NULL,
  ppv = NULL,
  interval = NULL,
  tol = 1e-08,
  allow_negative_validity = FALSE
)
```

Arguments

base_rate	Population proportion of successful applicants.
selection_ratio	Proportion selected.
validity	Predictor-criterion correlation.
ppv	Positive predictive value / success ratio among selected applicants.
interval	Search interval for the missing parameter.
tol	Numerical tolerance passed to `optimize()`.
allow_negative_validity	Logical. Should the solver allow negative validity when `validity = NULL`? Defaults to `FALSE`.

Value

A `psu_tr` object containing the solved parameter and the resulting Taylor-Russell table.

References

Taylor, H. C., & Russell, J. T. (1939). The relationship of validity coefficients to the practical effectiveness of tests in selection. Journal of Applied Psychology, 23, 565-578.

Waller, N. G. (2024). TaylorRussell: A Taylor-Russell function for multiple predictors (R package version 1.2.1). CRAN.

Examples

```
# Literature: Taylor and Russell (1939); Waller (2024).
# Use the first call as a minimal example; the longer block illustrates
# how to interpret the function in the substantive setting discussed in the literature.
# Minimal example: solve validity from desired PPV.
tr_solve(base_rate = .50, selection_ratio = .20, validity = NULL, ppv = .70)

# Substantive example (Taylor and Russell, 1939; Waller, 2024).
# Solve the selection ratio needed for a desired PPV.
tr_solve(base_rate = .50, selection_ratio = NULL, validity = .35, ppv = .70)
```

---

utility_fairness_frontier

Utility-fairness Pareto frontier

Description

Convenience wrapper around `pareto_frontier()` for selection-system alternatives evaluated on utility, fairness, and optionally validity.

Usage

```
utility_fairness_frontier(utility, fairness, validity = NULL)
```

Arguments

utility	Numeric vector of utility values to maximize.
fairness	Numeric vector of fairness values to maximize, for example an adverse-impact ratio where larger values indicate smaller subgroup disparity.
validity	Optional numeric vector of validity values to maximize.

Value

A data frame with frontier membership.

References

De Corte, W., Lievens, F., & Sackett, P. R. (2007). Combining predictors to achieve optimal trade-offs between selection quality and adverse impact. Journal of Applied Psychology, 92, 1380-1393.

Tippins, N. T., Oswald, F. L., & McPhail, S. M. (2021). Scientific, legal, and ethical concerns about AI-based personnel selection tools: A call to action. Personnel Assessment and Decisions, 7(2), Article 1.

Examples

```
# Literature: De Corte, Lievens, and Sackett (2007); Tippins, Oswald, and McPhail (2021).
utility_fairness_frontier(utility = c(100, 120, 90), fairness = c(.80, .70, .95))
```

---

utility_monte_carlo *Monte Carlo uncertainty propagation for BCG utility*

Description

Samples validity and SDy and propagates them through the BCG model. This is a simple decision-support approximation, not a full Bayesian model.

Usage

```
utility_monte_carlo(
  n_sim = 10000,
  validity_mean,
  validity_se,
  sdy_mean,
  sdy_sd,
  selection_ratio,
  n_selected,
  tenure,
  cost = 0,
  baseline_validity = 0,
  seed = NULL
)
```

Arguments

- `n_sim` Number of simulations.
- `validity_mean` Mean validity.
- `validity_se` Standard error of validity.
- `sdy_mean` Mean SDy.
- `sdy_sd` Standard deviation of SDy uncertainty.
- `selection_ratio` Selection ratio.
- `n_selected` Number selected.
- `tenure` Expected tenure.
- `cost` Cost.
- `baseline_validity` Baseline validity.
- `seed` Optional random seed.

Value

A `psu_monte_carlo` object with draws and quantiles.

References

Alexander, R. A., & Barrick, M. R. (1987). Estimating the standard error of projected dollar gains in utility analysis. Journal of Applied Psychology, 72, 475-479.

Rich, J. R., & Boudreau, J. W. (1987). The effects of variability and risk on selection utility analysis. Personnel Psychology, 40, 55-84.

Ock, J., & Oswald, F. L. (2018). The utility of personnel selection decisions: Comparing compensatory and multiple-hurdle selection models. Journal of Personnel Psychology, 17(4), 172-182.

Examples

```
# Literature: Alexander and Barrick (1987); Rich and Boudreau (1987); Ock and Oswald (2018).
# Use the first call as a minimal example; the longer block illustrates
# how to interpret the function in the substantive setting discussed in the literature.
# Minimal example (Alexander and Barrick (1987); Rich and Boudreau (1987); Ock and Oswald (2018)).
utility_monte_carlo(n_sim = 1000, validity_mean = .35, validity_se = .05,
                    sdy_mean = 50000, sdy_sd = 10000, selection_ratio = .20,
                    n_selected = 100, tenure = 3, cost = 75000, seed = 1)

# Substantive example (Alexander and Barrick, 1987;
# Rich and Boudreau, 1987; Ock and Oswald, 2018).
# Quantify the probability that net utility is positive.
mc <- utility_monte_carlo(n_sim = 2000, validity_mean = .30, validity_se = .06,
                          sdy_mean = 50000, sdy_sd = 15000,
                          selection_ratio = .20, n_selected = 100,
                          tenure = 3, cost = 75000,
                          baseline_validity = .15, seed = 123)
mc$probability_positive
```

utility_regression_diagnostics *Basic utility-analysis regression diagnostics*

Description

Fits a simple linear model and returns empirical inputs and normality checks relevant to linear utility analysis.

Usage

```
utility_regression_diagnostics(x, y)
```

Arguments

x	Predictor scores.
y	Criterion scores in raw or monetary units.

Value

A list with sample size, validity, SDy, regression coefficients, residual summaries, optional Shapiro-Wilk tests, and the fitted model.

References

Holling, H. (1998). Utility analysis of personnel selection: An overview and empirical study based on objective performance measures. Methods of Psychological Research Online, 3(1), 5-24.

Examples

```
# Literature: Holling (1998).
utility_regression_diagnostics(1:10, c(2, 3, 3, 5, 4, 6, 7, 8, 8, 10))
```

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